

Probability

Solved Example

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$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

| Example 01

- In a process that manufactures aluminum cans, the probability that a can has a flaw on its side is **0.02**, the probability that a can has a **flaw on the top** is **0.03**, and the probability that a can has a **flaw on both the side and the top** is **0.01**. What is the probability that a randomly chosen can has a flaw? What is the probability that it has no flaw?

$$P(\text{flaw on side}) = 0.02$$

$$P(\text{flaw on top}) = 0.03$$

$$P(\text{flaw on side and flaw on top}) = 0.01$$

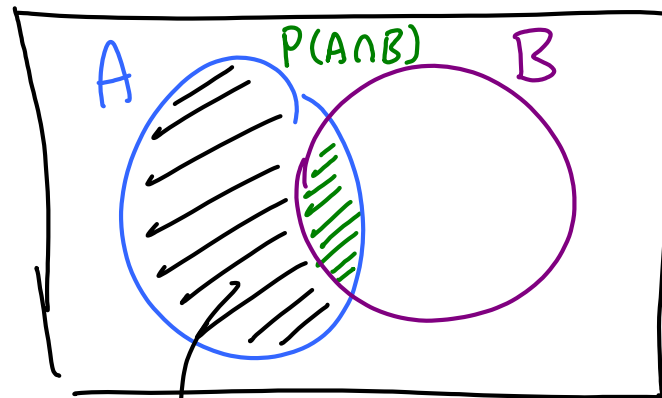
$$\begin{aligned} & P(\text{flaw on side } \underline{\text{or}} \text{ flaw on top}) = \\ & P(\text{flaw on side}) + \\ & P(\text{flaw on top}) - \\ & P(\text{flaw on side and flaw on top}) \\ & = 0.02 + 0.03 - 0.01 \\ & = 0.04 \\ & P(\text{no flaw}) = 1 - 0.04 = 0.96 \end{aligned}$$

Example 02

- Refer to Example 01 listed above. What is the probability that a can has a flaw on the top but not on the side?

A $\Rightarrow$ flaw on top

B $\Rightarrow$ flaw on side



$$P(A) = P(A \cap B) + \underline{P(A \cap B^c)}$$

$$P(A - B)$$

$$P(A \cap B')$$

$$= P(A) - P(A \cap B)$$

$$= 0.03 - 0.01$$

$$= \boxed{0.02}$$

| References

- Understanding Boxplots <https://towardsdatascience.com/understanding-boxplots-5e2df7bcbd51>
- What does a box plot tell you?
<https://www.simplypsychology.org/boxplots.html>
- Statistics for Engineers and Scientists, Fourth Edition, William Navidi
Colorado School of Mines
- Khan Academy
<https://www.khanacademy.org/math/cc-sixth-grade-math/cc-6th-data-statistics/cc-6th-box-whisker-plots/v/constructing-a-box-and-whisker-plot>