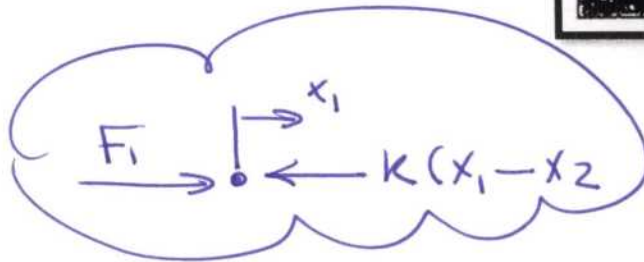
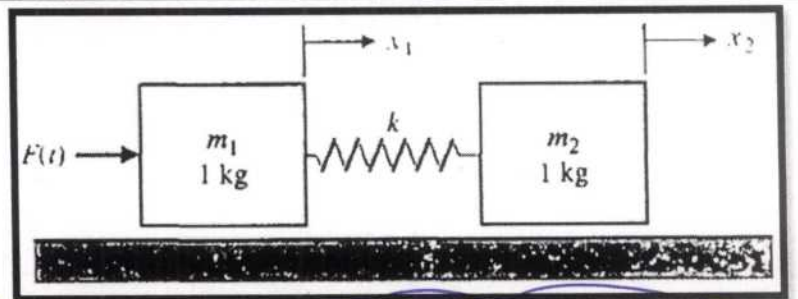


**Question No. (1) (10 Marks)**

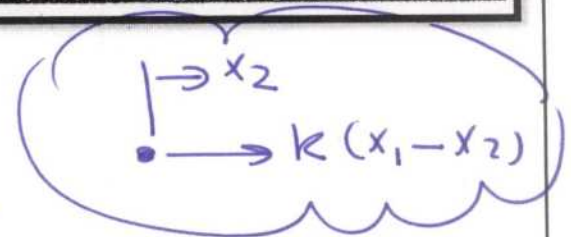
1. Determine the transfer function $X_2(s)/F(s)$ for the system shown in Figure below. Both masses slide on a frictionless surface, and $k = 1 \text{ N/m}$. Draw the Block diagram



$$F - k(x_1 - x_2) = m_1 s^2 x_1$$

$$F + kx_2 = (m_1 s^2 + k) x_1$$

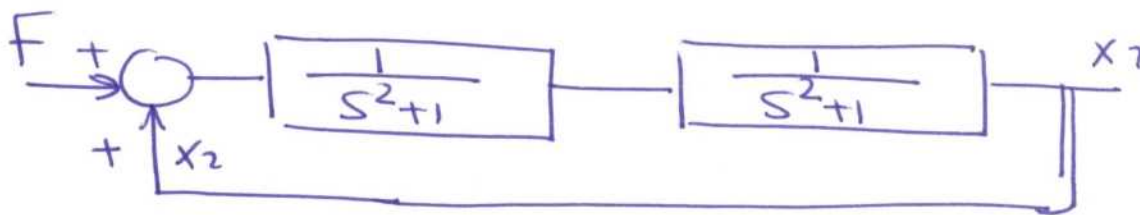
$$F + x_2 = (s^2 + 1) x_1$$



$$k(x_1 - x_2) = m_2 s^2 x_2$$

$$kx_1 = (m_2 s^2 + k) x_2$$

$$x_1 = (s^2 + 1) x_2$$



$$\frac{x_2}{F} = \frac{1}{(s^2 + 1)^2 - 1} = \frac{1}{(s^2 + 1 - 1)(s^2 + 1 + 1)}$$

$$\frac{x_2}{F} = \frac{1}{s(s^2 + 2)}$$

Question No. (2) (10 Marks)

Obtain the equation that relates the output voltage $Y(s)$ to $r(s)$ and $v_w(s)$

1st op-AMP

$$\frac{r}{R} - \frac{v_w}{R} = \frac{-e}{R}$$

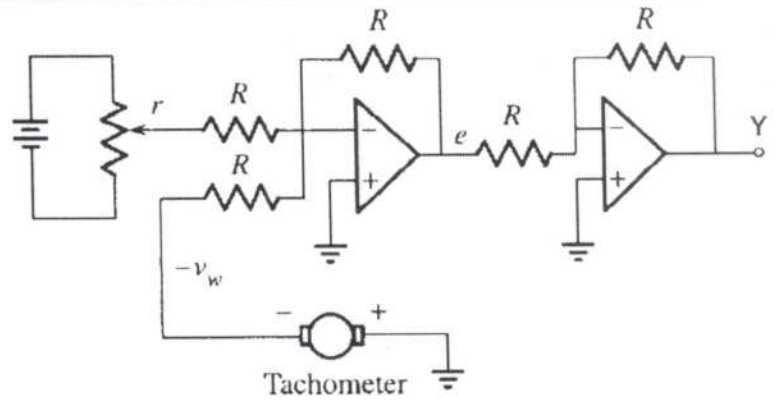
$$e = -(r - v_w)$$

2nd op-AMP

$$\frac{e}{R} = \frac{-Y}{R}$$

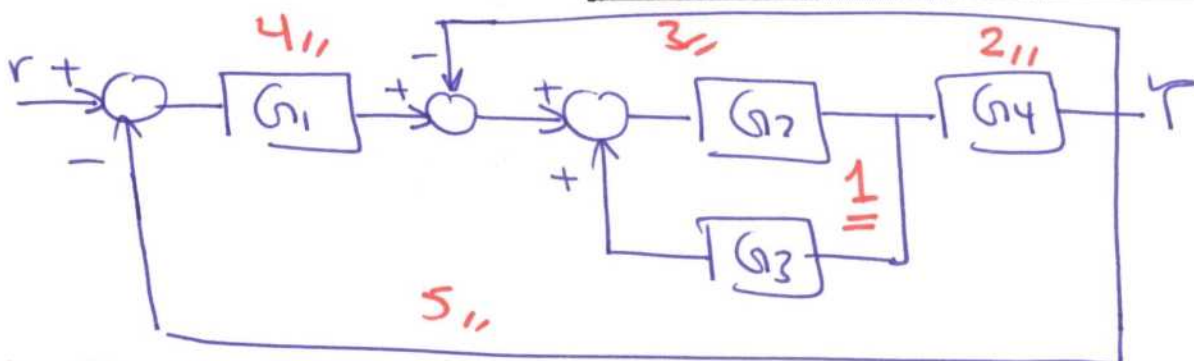
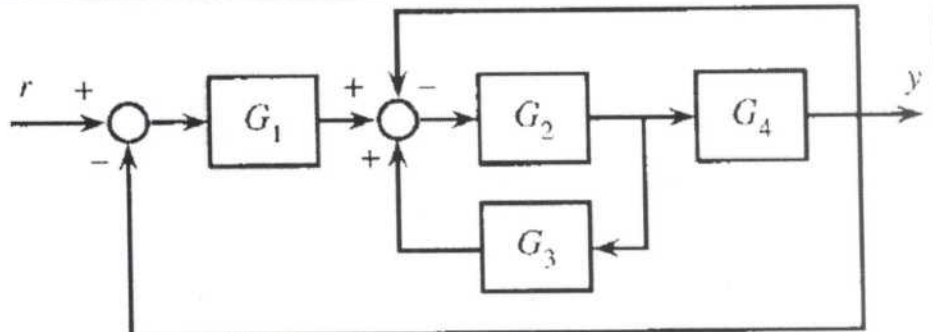
$$Y = -e$$

$$Y = r - v_w$$



Question No. (3) (10 Marks)

Use block manipulation to find the transfer function from r to y



1. Feedback 2. Series 3. Feedback 4. Series
5. Feedback

$$\frac{Y}{R} = \frac{G_4 G_2 G_1}{1 - G_2 G_3 + G_2 G_4 + G_1 G_2 G_4}$$

Question No. (4) (10 Marks)

Obtain the unit-step response of the following system:

$$\frac{C(s)}{R(s)} = \frac{10}{s^2 + 4s + 12}$$

$$r(t) = 1 \Rightarrow R(s) = 1/s$$

$$\begin{aligned} C(s) &= \frac{10}{s(s^2 + 4s + 12)} \\ &= \frac{10/12}{s} + \frac{As + B}{s^2 + 4s + 12} \end{aligned}$$

$$10 = \frac{10}{12} (s^2 + 4s + 12) + s(As + B)$$

$$\begin{aligned} \text{Coefficient of } s^2 &= 0 = \frac{10}{12} + A & A &\Rightarrow -\frac{10}{12} \\ \text{" of } s &= 0 = \frac{10}{3} + B & B &= -\frac{10}{3} \end{aligned}$$

$$\therefore C(s) = \frac{10/12}{s} - \frac{10}{12} \frac{s+4}{s^2 + 4s + 12}$$

$$C(s) = \frac{10/12}{s} - \frac{10}{12} \frac{(s+2)+2}{(s+2)^2 + 8}$$

$$C(s) = \frac{10/12}{s} - \frac{10}{12} \left[\frac{s+2}{(s+2)^2 + 8} + \frac{2}{\sqrt{8}} \frac{\sqrt{8}}{(s+2)^2 + 8} \right]$$

$$c(t) = \frac{10}{12} - \frac{10}{12} e^{-2t} \left(\cos \sqrt{8} t + \frac{1}{\sqrt{2}} \sin \sqrt{8} t \right)$$