

Probability

Solved Example

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| Example 01

- In a process that manufactures aluminum cans, the probability that a can has a **flaw on its side is 0.02**, the probability that a can has a **flaw on the top is 0.03**, and the probability that a can has a **flaw on both the side and the top is 0.01**. What is the probability that a randomly chosen can has a flaw? What is the probability that it has no flaw?

| Example

Solution

We are given that $P(\text{flaw on side}) = 0.02$, $P(\text{flaw on top}) = 0.03$, and $P(\text{flaw on side and flaw on top}) = 0.01$. Now $P(\text{flaw}) = P(\text{flaw on side or flaw on top})$. Using Equation (2.5),

$$\begin{aligned}P(\text{flaw on side or flaw on top}) &= P(\text{flaw on side}) + P(\text{flaw on top}) \\&\quad - P(\text{flaw on side and flaw on top}) \\&= 0.02 + 0.03 - 0.01 \\&= 0.04\end{aligned}$$

To find the probability that a can has no flaw, we compute

$$P(\text{no flaw}) = 1 - P(\text{flaw}) = 1 - 0.04 = 0.96$$

Venn diagrams can sometimes be useful in computing probabilities by showing how to express an event as the union of disjoint events. Example 2.9 illustrates the method.

| Example 02

- Refer to Example 01 listed above. What is the probability that a can has a flaw on the top but not on the side?

| Note...

$$P(A^c) = 1 - P(A)$$

1- قاعدة المكمل
لأي حدث A

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

إذا كانت A, B أحداث متنافية فإن

$$P(A \cup B) = P(A) + P(B)$$

2- القاعدة الخاصة لجمع
الاحتمالات

إذا كان: A, B حدثين في فضاء
عينة فإن :

$$P(A - B) = P(A \cap B') = P(A) - P(A \cap B)$$

3- الفرق

| Example 02

- Refer to Example 01 listed above. What is the probability that a can has a flaw on the top but not on the side?

| References

- Understanding Boxplots <https://towardsdatascience.com/understanding-boxplots-5e2df7bcbd51>
- What does a box plot tell you?
<https://www.simplypsychology.org/boxplots.html>
- Statistics for Engineers and Scientists, Fourth Edition, William Navidi
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<https://www.khanacademy.org/math/cc-sixth-grade-math/cc-6th-data-statistics/cc-6th-box-whisker-plots/v/constructing-a-box-and-whisker-plot>